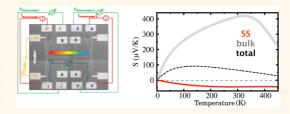
Impact of the Topological Surface State on the Thermoelectric Transport in Sb₂Te₃ Thin Films

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ABSTRACT Ab initio electronic structure calculations based on density functional theory and tight-binding methods for the thermoelectric properties of *p*-type Sb₂Te₃ films are presented. The thickness-dependent electrical conductivity and the thermopower are computed in the diffusive limit of transport based on the Boltzmann equation. Contributions of the bulk and the surface to the transport coefficients are separated, which enables to identify a clear impact of the topological surface state on the thermoelectric properties. When the charge



carrier concentration is tuned, a crossover between a surface-state-dominant and a Fuchs-Sondheimer transport regime is achieved. The calculations are corroborated by thermoelectric transport measurements on Sb₂Te₃ films grown by atomic layer deposition.

KEYWORDS: topological insulators · thermoelectrics · thin films · density functional theory (DFT) · atomic layer deposition (ALD) · surface states · thermopower · four-terminal measurements

lmost all proposed three-dimensional (3D) Z_2 topological insulators (Tls)^{1,2} are efficient thermoelectric materials. That is not by coincidence, since the link between an efficient thermoelectric material and the topological character is the inverted band gap.^{3,4} The last is due to spin-orbit coupling which switches parity of the bands and leads, if strong enough, to narrow band gaps which are favorable for efficient room-temperature thermoelectrics. Usually, strong spin-orbit coupling is mediated by heavy elements, which in turn also tend to reduce the material's lattice thermal conductivity, another requirement for desirable thermoelectrics.

In the early 90s, Hicks and Dresselhaus^{5,6} proposed the concept of low-dimensionality to increase further the thermoelectric efficiency; primarily in thin films, the thermopower *S* should be enlarged. However, in contrast to previous theoretical model calculations,^{7,8} decreased values of *S* were found experimentally^{9–11} for Bi₂Te₃ and Sb₂Te₃ thin films and were recently corroborated by both model^{12,13} and *ab initio* calculations⁴ of our groups. Thus, to resolve this discrepancy, the potential impact of the surface state (SS) of TIs on thermoelectricity needs to be investigated in more detail. In this Article, we present *ab initio* calculations and transport measurements of the thermoelectric properties of Sb_2Te_3 films at varying thickness, temperature, and charge carrier concentration.

RESULTS

Theoretical Results. In the following, we discuss the doping- and temperature-dependent electrical conductivity and thermopower, as shown in Figure 1, exemplary for a Sb₂Te₃ film with thickness of 18 quintuple-layer (QL), *i.e.*, about 18 nm. A discussion of films with other thicknesses is given in the Supporting Information.¹⁴

The converged electronic structure results serve as input to obtain the thermoelectric transport properties at temperature T and fixed extrinsic charge carrier concentration p by solving the linearized Boltzmann equation in relaxation time approximation (RTA).¹⁵ By using special projection techniques,⁴ we distinguish between contributions from bulk states (gray

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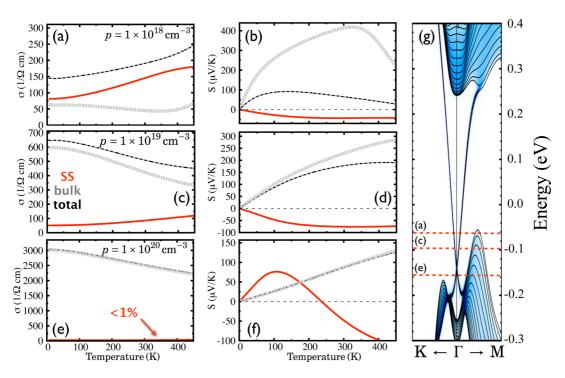


Figure 1. Electrical conductivity (a, c, and e) and thermopower (b, d, and f) in dependence on temperature for three distinct hole concentrations at a film thickness of 18 QL. Hole concentration $n = 1 \times 10^{18}$ cm⁻³ in (a) and (b), $p = 1 \times 10^{19}$ cm⁻³ in (c) and (d), $p = 1 \times 10^{20}$ cm⁻³ in (e) and (f). Pure bulk contributions are represented by gray dashed lines; the contribution of the surface states is given by red solid lines, while black dash-dotted lines show the total contribution of the sample. In (g) the band structure of the 18 QL Sb₂Te₃ film is shown around the fundamental band gap. Thin red dashed lines indicate the position of the chemical potential μ at zero temperature.

dashed lines), SSs (red solid lines), and the total contribution (black dash-dotted line), defined as $\sigma_{tot} = \sigma_{bulk} + \sigma_{SS}$ and $S_{tot} = (\sigma_{bulk}S_{bulk} + \sigma_{SS}S_{SS})/\sigma_{tot}$. Three typical charge carrier concentrations are chosen to reflect the overall behavior of the transport properties. Only *p*-type thin films will be discussed because Sb₂Te₃ is inherently *p*-type conductive^{16,17} due to intrinsic defects, *i.e.*, Sb vacancies, Sb_{Te} antisites, and Sb–Te₁ exchange defects.

Due to the fact that a 3D TI offers robust metallic SSs (we denote the SS metallic, as it shows clear transport signatures of a conventional metal) within the insulating bulk band gap, an enhanced electrical conductivity of the entire system compared to a conventional insulator is expected for very small charge carrier concentrations, i.e., if the chemical potential is situated in or nearby the bulk band gap. The latter scenario is shown in Figure 1a for a *p*-type doping of $p = 1 \times$ 10^{18} cm⁻³. At low temperatures, the contribution σ_{SS} of the SS (red solid line) is already larger than the bulk contribution $\sigma_{\rm bulk}$. With increasing temperature, the chemical potential shifts into the band gap, thereby decreasing $\sigma_{\rm bulk}$ until bipolar conduction contributes at about T = 300 K. In contrast, σ_{ss} increases monotonically with temperature. The latter can easily be understood, having in mind that for a two-dimensional system, *i.e.*, the SS, the transport distribution function (TDF) scales as $\Sigma(\mu) \propto dl_{\rm F} \times v$, where $dl_{\rm F}$ is the circumference of the Fermi circle at chemical potential μ .

For energies close to the Dirac point, v_{SS} is constant in energy, while $dI_F \propto E$. Consequently, the TDF is linear in energy. Small deviations from the latter arise at about $E \approx 0.1$ eV and are attributed to the hexagonal warping of the Fermi surface.

The impact of the SS on the total thermopower, as shown in Figure 1b, is even more remarkable. While the bulk contribution S_{bulk} shows the typical behavior for a p-type narrow-band gap semiconductor with a maximum of $S_{\text{bulk}} \approx 410 \,\mu\text{V/K}$ at T = 325 K, the contribution of the SS shows the expected metallic behavior with small values of $S_{\text{SS}} \leq -50 \,\mu\text{V/K}$. The negative sign stems from the mere fact that the SS above (below) the Dirac point mimics the slope of the band dispersion of conduction (valence) bands.

Summarizing, the influence of the SS leads to a clearly diminished total thermopower (black dash-dotted line). As a rule of thumb, assuming $S_{\text{bulk}} \gg S_{\text{SS}}$ yields $S_{\text{tot}} \approx S_{\text{bulk}}/(\eta + 1)$ with $\eta = \sigma_{\text{SS}}/\sigma_{\text{bulk}}$. The larger the contribution of the SS to the total electrical conductivity, the smaller the total thermopower S_{tot} .

The value of the total thermopower (65 μ V/K at 300 K; black dashed-dotted line in Figure 1b) is reduced to less than one-fifth of the bulk value, which corroborates the above-noted estimation. We note that, within the RTA, the signature of the SS on S_{tot} relies to a certain extent on the ratio τ_{SS}/τ_{bulk} of the relaxation times. If $\tau_{bulk} \gg \tau_{SS}$, the reduction of the total thermopower due to the conducting SS would be much weaker than

VOL.9 • NO.4 • 4406-4411 • 2015 AC

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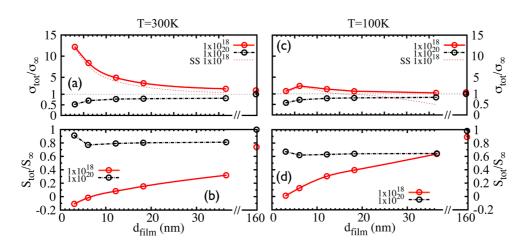


Figure 2. Thickness-dependent thermoelectric transport properties. Total electrical conductivity and thermopower at T = 300 K (a and b) and T = 100 K (c and d), respectively. The results are depicted for two distinct hole concentrations: $p = 1 \times 10^{18}$ cm⁻³ (red solid lines) and $p = 1 \times 10^{20}$ cm⁻³ (black dash-dotted lines). For the electrical conductivity in (a) and (c), the pure contribution of the surface state is given additionally as a thin dashed red line. All the transport properties are normalized to the bulk values σ_{∞} and S_{∞} .

proposed. With regard to the backscattering protection of the SS, however, the opposite scenario $\tau_{SS} \gg$ $\tau_{\rm bulk}$ should be expected.¹⁸

For thermoelectric applications charge carrier concentration of $p = 1 \times 10^{19} \text{ cm}^{-3}$ (cf. Figure 1, panels c and d) are more applicable. Here the contribution of the SS to $\sigma_{\rm tot}$ is smaller, compared to the low doped case, as the chemical potential is located closer to the Dirac point (cf. Figure 1c). Still, a reduction of the film's total thermopower by 45% to $S_{\rm tot} \approx$ 187 μ V/K at T = 400 K compared to the bare bulk value is calculated due to the impact of the metallic SS (cf. Figure 1d).

In heavy p-doped samples, at $p = 1 \times 10^{20}$ cm⁻³, as depicted in Figure 1, panels e and f, the absolute value of S_{SS} still reaches about 25 (Ω cm)⁻¹ at room temperature but is negligibly small compared to the bulk contribution. This is reflected in the thermopower, for which $S_{tot} \approx S_{bulk}$. Focusing on the SS contribution, the picture is more delicate. At low temperatures, S_{SS} is positive but decreases at elevated temperatures and changes sign at about T = 250 K. The latter is attributed to a shift of the chemical potential above the Dirac point, where the slope of both the TDF and S_{SS} change sign.

After discussing the temperature and dopingdependent thermoelectric transport properties for a film of 18 QL thickness, we now focus on the film thickness dependence of the transport properties at T = 300 K and T = 100 K, as shown in Figure 2. At roomtemperature, two distinct transport regimes can be discussed with respect to the dependence of the charge carrier concentration of the films. At heavy *p*-doping ($p = 1 \times 10^{20}$ cm⁻³, black dash-dotted lines in Figure 2), the film behaves almost metallic without significant influence of the topological SS on the transport properties. With increasing film thickness the normalized electrical conductivity at room temperature (cf. Figure 2a) tends asymptotically to the bulk value as $(\sigma_{tot}/\sigma_{\infty}) \sim (1 + (3v\tau/8d))^{-1}$ in accordance

with the Fuchs-Sondheimer theory.^{19,20} While derived to describe surfaces the Fuchs-Sondheimer theory does not account for the influence of SSs and quantum size effects. As previously described, these can be probed at low charge carrier concentrations ($p = 1 \times$ 10^{18} cm⁻³, red solid lines in Figure 2). As shown in Figure 2a, the behavior of the total electrical conductivity than differs evidently from the Fuchs-Sondheimer limit. At low film thickness we find enhanced values of $(\sigma_{\rm tot}/\sigma_{\infty}) \approx$ 12. Obviously the contributions of the SSs dominate the transport and lift the total electrical conductivity above the bulk limit. As indicated in Figure 2a, the contribution of the SS to the total transport exceeds 90% (cf. the thin red dashed lines). A comparable crossover between surface statedominated and Fuchs-Sondheimer transport was reported for ultrathin copper films.²¹ Generally speaking, for film thicknesses above 18 QL thickness, the k-dependency and spatial distribution of the surface states is fully established. Thus, the surface contribution to the transport properties remain robust for thicker films and the TDF scales as $\Sigma_{SS}(d) \sim (1/d)$. Quantum confinement effects are hardly visible for the 160 QL film, *i.e.*, $\sigma_{\text{bulk}}(d) \approx \sigma_{\infty}$ and $\sigma_{\text{tot}}(d) \approx \sigma_{\infty} + \sigma_{\infty}$ $(\sigma_{\varsigma\varsigma}/d)$.

The dependence of the normalized total thermopower on the film thickness is presented in Figure 2b,d. Keeping in mind the aforementioned relation $S_{\rm tot}/S_{\infty} \approx$ $(\sigma_{\infty} + \sigma_{SS} \times (S_{SS}/S_{\infty})) / \sigma_{tot} / S_{tot} / S_{\infty} \le 1$ can be expected for a broad range of temperatures and doping in the thin TI films. (We note that there is a difference of S_{bulk} and S_{∞} , which are the bulk contribution to a thin film and the contribution of a perfect infinite bulk, respectively. However, $S_{\text{bulk}} = S_{\infty}$ is used in this estimation and is valid for qualitative discussions.) This is related to the mere fact, that in a TI the SS is metallic, hence showing small values of |S_{SS}|, while the bulk is insulating yielding large values of $|S_{\infty}|$. The position of the Dirac point near

VOL.9 NO.4 4406-4411 2015

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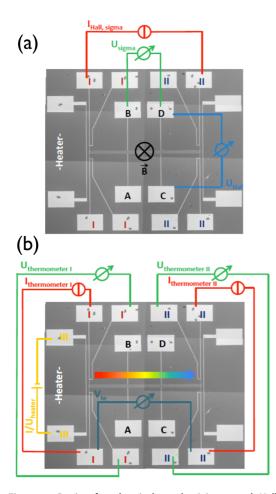


Figure 3. Device for electrical conductivity σ and Hall measurements (a) as well as for determining the Seebeck coefficient $S = V_{\text{th}}/(T_1 - T_{11})$ (b) of a Sb₂Te₃ thin film. The magnetic field B is applied perpendicular to the film plane. Bright lines are lithographically defined metal lines used as heater, as ohmic inner electrodes for electric measurements and as resistive thermometers, as indicated (see Methods for details).

the band edge, *i.e.*, the case in Sb₂Te₃ and Bi₂Te₃, leads moreover to opposite signs of S_{SS} and S_{∞} , further reducing S_{tot}/S_{∞} .

Occasionally, the bulk and the SS's contribution have the same sign and $S_{SS} > S_{oo}$, leading to an enlarged $S_{tot}/S_{oo} > 1$. The latter scenario is seen in Figure 1f for a heavily *p*-doped sample at temperatures lower than T = 180 K. However, as these situations occur only if the bulk is metallic, *i.e.*, $\sigma_{bulk} \gg \sigma_{SS}$, the total thermopower will not exceed the bulk limit considerably, yielding $S_{tot} \approx S_{oo}$.

Experimental Results. To support our theoretical findings at room temperature, experimental four-terminal measurements (see Figure 3 and Methods) on the normalized total electrical conductivity and total thermopower at varying Sb₂Te₃ film thickness are presented in Figure 4. As can be seen from Figure 4b, the total thermopower tends asymptotically toward the bulk limit for increasing film thickness, *i.e.*, decreasing influence of the SSs, in accordance to the

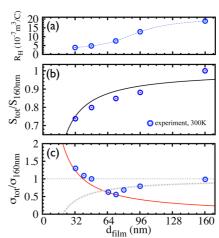


Figure 4. Measured thickness dependent thermoelectric transport properties at room temperature. Shown (as blue dots) is the normalized total thermopower (b) and the normalized total electrical conductivity (c) for varying film thickness. The charge carrier concentration varies monotonically with film thickness (a). Hence, the two transport regimes are superimposed in the experiment. The surface-state dominant regime (red solid line) and a Fuchs-Sondheimer transport regime (gray dashed line). The total thermopower (b) is always reduced due to the contribution of the surface-states.

theoretical calculations in Figure 2b (preferably red solid line). Obviously the measured Hall coefficient $R_{\rm H}$ is not a constant with the film thickness (Figure 4a). Within a two channel model for $R_{\rm H}^{14,22}$ and mobilities $\mu_{\rm SS} \approx \mu_{\rm bulk}$, ^{14,23} the charge carrier concentration p of the thin films slightly varies monotonically with the number of deposited layers, too. That allows for direct observation of the transition between the surface-state-dominant and Fuchs-Sondheimer transport regime of the total electrical conductivity, shown in Figure 4c.

At low film thickness, d < 48 nm and still low enough charge carrier concentrations the SSs noticeably influence the transport, i.e., the normalized total electrical conductivity is higher than expected from the bare bulk sample (indicated by red solid lines). With increasing film thickness, the influence of the SSs is suppressed and bulk states dominate the transport. Nevertheless, the low charge carrier concentrations allow to see influences in the thermopower even at large film thicknesses, as pointed out in Figure 2b. Starting from a quantum mechanical approach, a Fuchs-Sondheimer transport regime can be expected (indicated by gray dashed lines), with the normalized total electrical conductivity tending to the bulk value for large film thickness. Clearly the measured data supports qualitatively all aspects of the theoretical calculations; hence, $\mu_{SS} \approx \mu_{bulk}$ is strongly expected.

To close our discussions, we point to the low temperature case of T = 100 K shown in Figure 2b,d. While the main trends remain and the same conclusions as for the room-temperature case can be drawn, the influence of the SS on the total electrical

VOL.9 • NO.4 • 4406-4411 • 2015

agnanc www.acsnano.org conductivity being diminished (*cf.* Figure 2c). Two facts lead to this result: (*i*) the chemical potential is located deeper in the valence bands for a given charge carrier concentration and (*ii*) the broadening of the Fermi—Dirac distribution in eq 1 is reduced. Both facts lead to a reduced influence of the SSs located in the fundamental band gap. Deviations are only found for ultrathin films of 3 QL thickness, for which the hybridization of the SSs at opposite sides of the film opens up gaps in the SS bands; at low temperature both the SS and the bulk interior behave then like a conventional semiconductor.^{8,12,14}

CONCLUSION

Combining quantum theoretical methods and experimental techniques on thin-film Sb_2Te_3 , we reproduced and clarified the reduction the total thermopower found in various experiments on thin-film thermoelectric TIs.^{9–11} By means of *ab initio* electronic structure calculations based on density functional

METHODS

Computational Details. The transport properties of the Sb_2Te_3 films are calculated in the diffusive limit of transport by means of the semiclassical Boltzmann equation in relaxation time approximation (RTA).^{15,24} Within this approximation we assume that the attached heaters and metallic leads basically preserve the surface band structure.

The basis of the transport calculations, *i.e.*, the atomistic structure, was simulated by slabs of 15 to 800 atomic layers, *i.e.*, three -160 QL Sb₂Te₃. The experimental in-plane lattice parameter $a_{\rm SbTe}^{\rm hex} = 4.264$ Å and relaxed atomic positions²⁵ were used.

The electronic structures of the Sb₂Te₃ films were obtained by first-principles calculations within density functional theory (DFT), as implemented in the QuantumEspresso code.²⁶ Fully relativistic, norm-conserving pseudopotentials were used; exchange and correlation effects were accurately accounted for by the local density approximation (LDA).²⁷

Subsequently, the first-principles electronic structures were mapped onto tight-binding Hamiltonians.^{28,29} The resulting band structures were checked against our first-principles Korringa-Kohn-Rostoker^{24,30} and QuantumEspresso results and yield fine agreement, in particular for the energy range near the fundamental band gap.

The electronic structures serves as an input to obtain the thermoelectric transport properties, using the layer-resolved transport distribution function (TDF) $\Sigma_i(\mu) = \mathscr{L}_i^{(0)}(\mu, 0)$.³¹ The generalized conductance moments $\mathscr{L}_i^{(n)}(\mu, T)$ are defined as

$$\mathcal{L}_{i}^{(n)}(\mu,T) = \frac{\tau}{(2\pi)^{2}} \sum_{\nu} \int d^{2}\mathbf{k} |v_{\mathbf{k}}^{\nu}|^{2}$$

$$\mathcal{L}_{\mathbf{k}}^{i} (E_{\mathbf{k}}^{\nu} - \mu)^{n} \left(-\frac{\partial f(\mu,T)}{\partial E} \right)_{E=E_{\mathbf{k}}^{\nu}}$$
(1)

 v_{k}^{\prime} denotes the group velocities in the directions of the hexagonal basal plane and \mathscr{P}_{k}^{\prime} is the layer-resolved probability amplitude of a Bloch state, which allows for spatial decomposition of the transport properties.³² Details on this projection technique are published elsewhere.⁴ The relaxation time for Sb₂Te₃ was fitted to experimental data and chosen constant with absolute value $\tau = 12$ fs with respect to wave vector **k** and energy on the scale of $k_{B}T.^{24}$ The influence of electron – phonon coupling was theoretically and experimentally found to be very weak and is discussed in detail in ref 4. Assuming stoichiometric

theory, we discussed the thermoelectric properties of the *p*-type TI Sb₂Te₃ for various film thicknesses and temperatures. The topologically protected surfacestate leads to metallic conduction of the thin films even in the semiconducting regime. As shown by a separation of bulk and surface contributions, the latter leads to a strong reduction of the total measured thermopower of the thin films. This reduction is present in a wide range of film thicknesses and doping. When we vary the charge carrier concentration a crossover between a surface-state-dominant and a Fuchs-Sondheimer transport regime is achieved. These two transport regimes, as well as a reduction of the total thermopower with decreasing film thickness are confirmed by thermoelectric transport measurements

samples, exchange-defects of Sb and Te₁ are the most probable scattering centers to be expected.¹⁶ Thus, electron-impurity scattering will dominate. We checked the state-dependency of electron-impurity relaxation time τ_k in Born approximation¹⁴ and found a constant Brillouin zone averaged value of τ to be a reasonable approximation. The temperature- and doping-dependent in-plane electrical conductivity σ and thermopower *S* read

on atomic layer deposited Sb₂Te₃ thin films. To gain

a thermoelectric benefit from thin film topological

insulators, gapping the surface state at low tempera-

tures and charge carrier concentrations seems to be

the only favorable ansatz.

$$\sigma = 2e^2 \mathcal{J}^{(0)}(\mu, T) \text{ and } S = \frac{1}{eT} \frac{\mathcal{J}^{(1)}(\mu, T)}{\mathcal{J}^{(0)}(\mu, T)}$$
 (2)

for given chemical potential μ at temperature ${\it T}$ and fixed extrinsic carrier concentration.

The combination of first-principles and related tight-binding calculations allows for dense adaptive k-point meshes to ensure the convergence of eq 1.^{30,33} The calculation consists of more than 500 points in a piece of the 2D Fermi surface in the irreducible part of the Brillouin zone (BZ).

Experimental Details. The Sb_2Te_3 thin films were grown on silicon wafers with a top layer of 300 nm SiO₂ via Atomic Layer Deposition (ALD) at substrate temperatures of 353 K. (Et₃Si₂)Te and SbCl₃ were used as precursors at source temperatures of 350 and 328 K, respectively.³⁴ For the transport measurements, the Sb₂Te₃ thin films were deposited on a lithographically prepatterned Hall bar, which was defined via laser beam lithography and subsequent developing of the exposed photoresist. Contacts to the hall bars were defined in a second lithography step, prior to sputter deposition of Ti/Pt metal contacts. The thickness t and lateral dimensions (length l, width w) of the films were obtained by Atomic Force Microscopy and SEM images, respectively (cf. Supporting Information). The Hall resistance $R_{\rm H} = U_{\rm C,D}/I_{\rm LH}$ of the films was determined with standard lock-in technique. A constant ac current with an amplitude of I_{LII} = 10 μA and frequency of 6 Hz was applied along the film stripe between contacts I and II and the voltage drop $U_{C,D}$ across the film width has been measured between contacts C and D, while sweeping a magnetic field from -3 to 3 T in 0.1 T steps (cf. Figure 3a). The magnetic field has been applied perpendicular to the film plane. The electrical conductivity has been calculated using $\sigma = [l/wt]/R_{\rm H}$ where $R_{\rm H} = U_{\rm C,D}/l_{\rm L,H}$ is the resistance of the film, measured in a four-point configuration between contacts B and D. To determine the Seebeck coefficient $S = V_{th}/\Delta T$ of the films the on-chip line heater generated a temperature difference ΔT across its length.

VOL.9 NO.4 4406-4411 2015 A

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 ΔT was measured by resistance thermometry using two metal four-probe thermometer lines (I and II) located at the film ends (cf. Figure 3b), which were driven by standard lock-in technique in a four-terminal configuration.^{11,35} The metal lines for thermometry also served as electrodes for measuring $V_{\rm th}$. Expected error bars for film thickness, thermopower and electrical conductivity are \sim 10%, \sim 16%, and \sim 7%, respectively.

Conflict of Interest: The authors declare no competing financial interest.

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Supporting Information Available: Additional results on the doping- and temperature-dependent electrical conductivity and thermopower for other film thicknesses, informations on the electronic structure at varying film thickness, as well as structural analysis of the ALD grown thin films are available online. T This material is available free of charge via the Internet at http://pubs.acs.org.

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